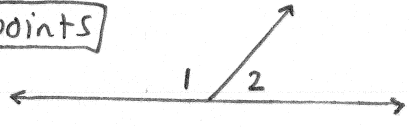
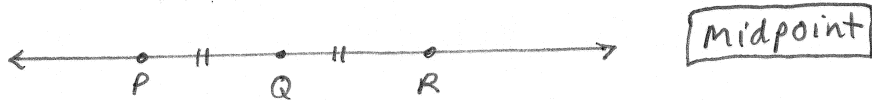


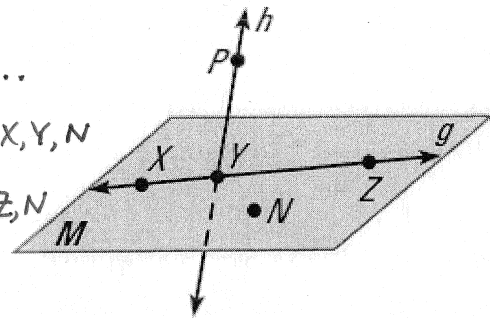
**VOCABULARY EXERCISES**

- Copy and complete: Points A and B are the ? of  $\overline{AB}$ . Endpoints
- Draw an example of a *linear pair*.  $\angle 1$  and  $\angle 2$  are a linear pair. 
- If Q is between points P and R on  $\overline{PR}$ , and  $PQ = QR$ , then Q is the ? of  $\overline{PR}$ .



**EXERCISES**

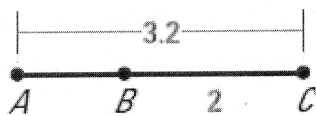
- Give another name for line g. Ex:  $\overleftrightarrow{XZ}$ ;  $\overleftrightarrow{YX}$ ;  $\overleftrightarrow{ZY}$ ...
- Name three points that are *not* collinear. Ex: Points X, Y, N
- Name four points that are coplanar. Ex: Points X, Y, Z, N
- Name a pair of opposite rays.  $\overrightarrow{YX}$  and  $\overrightarrow{YZ}$
- Name the intersection of line h and plane M.



Point Y

Find the indicated length.

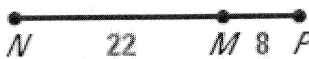
9. Find AB.



$$AB + 2 = 3.2$$

$AB = 1.2$

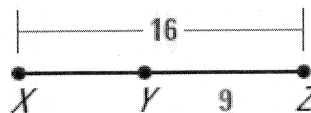
10. Find NP.



$$22 + 8 = NP$$

$NP = 30$

11. Find XY.



$$XY + 9 = 16$$

$XY = 7$

12. The endpoints of  $\overline{DE}$  are  $D(-4, 11)$  and  $E(-4, -13)$ . The endpoints of  $\overline{GH}$  are  $G(-14, 5)$  and  $H(-9, 5)$ . Are  $\overline{DE}$  and  $\overline{GH}$  congruent? Explain.

$$DE = \sqrt{(-4 - -4)^2 + (-13 - 11)^2}$$

$$= \sqrt{0^2 + (-24)^2}$$

$$DE = 24$$

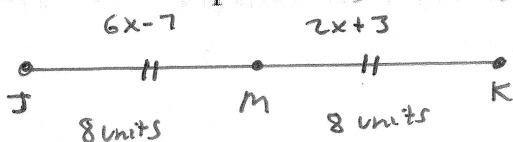
$$GH = \sqrt{(-9 - -14)^2 + (5 - 5)^2}$$

$$= \sqrt{5^2 + 0^2}$$

$$GH = 5$$

The segments are not  $\cong$ , as their lengths are not equal.

13. Point M is the midpoint of  $\overline{JK}$ . Find JK when  $JM = 6x - 7$  and  $MK = 2x + 3$ .



$$6x - 7 = 2x + 3$$

$$4x = 10$$

$x = 2.5$

$JK = 16$

In Exercises 14-17, the endpoints of a segment are given. Find the length of the segment rounded to the nearest tenth. Then find the coordinates of the midpoint of the segment.

14.  $A(2, 5)$  and  $B(4, 3)$

$$d = \sqrt{(4-2)^2 + (3-5)^2} = \sqrt{2^2 + (-2)^2} = \sqrt{8}$$

$$AB = \boxed{2\sqrt{2} \approx 2.83}$$

$$\left( \frac{2+4}{2}, \frac{5+3}{2} \right) = \left( \frac{6}{2}, \frac{8}{2} \right) = (3, 4)$$

Midpoint Coordinate:  $(3, 4)$

15.  $F(1, 7)$  and  $G(6, 0)$

$$d = \sqrt{(6-1)^2 + (0-7)^2} = \sqrt{5^2 + (-7)^2} = \sqrt{74}$$

$$FG = \boxed{\sqrt{74} \approx 8.60}$$

$$\left( \frac{1+6}{2}, \frac{7+0}{2} \right) = \left( \frac{7}{2}, \frac{7}{2} \right) = (3.5, 3.5)$$

Midpoint Coordinate:  $(3.5, 3.5)$

16.  $H(-3, 9)$  and  $J(5, 4)$

$$d = \sqrt{(5-(-3))^2 + (4-9)^2} = \sqrt{8^2 + (-5)^2} = \sqrt{89}$$

$$HJ = \boxed{\sqrt{89} \approx 9.43}$$

$$\left( \frac{-3+5}{2}, \frac{9+4}{2} \right) = \left( \frac{2}{2}, \frac{13}{2} \right) = (1, 6.5)$$

Midpoint Coordinate:  $(1, 6.5)$

17.  $K(10, 6)$  and  $L(0, -7)$

$$d = \sqrt{(0-10)^2 + (-7-6)^2} = \sqrt{(-10)^2 + (-13)^2} = \sqrt{269}$$

$$KL = \boxed{\sqrt{269} \approx 16.40}$$

$$\left( \frac{10+0}{2}, \frac{6+(-7)}{2} \right) = \left( \frac{10}{2}, \frac{-1}{2} \right) = (5, -0.5)$$

Midpoint Coordinate:  $(5, -0.5)$

18. Point  $C(3, 8)$  is the midpoint of  $\overline{AB}$ . One endpoint is  $A(-1, 5)$ . Find the coordinates of endpoint  $B$ .  $B(x_1, y_1)$

$$\frac{-1 + x_1}{2} = 3 \quad \left\{ \quad \frac{5 + y_1}{2} = 8 \right.$$

$$\frac{-1 + x_1}{2} = 6 \quad \left\{ \quad \frac{5 + y_1}{2} = 16 \right.$$

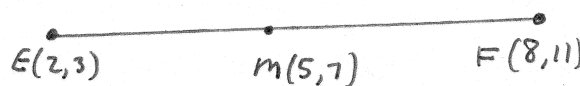
$$x_1 = 7 \quad \left\{ \quad y_1 = 11 \right.$$

$$\boxed{B(7, 11)}$$

19. The endpoints of  $\overline{EF}$  are  $E(2, 3)$  and  $F(8, 11)$ . The midpoint of  $\overline{EF}$  is  $M$ . Find the length of  $\overline{EM}$ .

$$d = \sqrt{(5-2)^2 + (7-3)^2} = \sqrt{3^2 + 4^2} = \sqrt{25} = 5$$

$$\boxed{EM = 5}$$



$$\left( \frac{2+8}{2}, \frac{3+11}{2} \right) = \left( \frac{10}{2}, \frac{14}{2} \right) = (5, 7)$$

20. In the diagram shown at the right,  $m\angle LMN = 140^\circ$ . Find  $m\angle PMN$ .  $11x - 9 + 5x + 5 = 140$

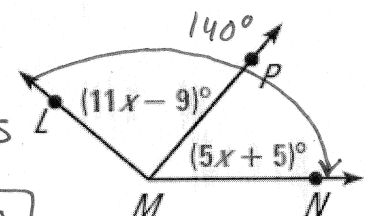
$$16x - 4 = 140$$

$$16x = 144$$

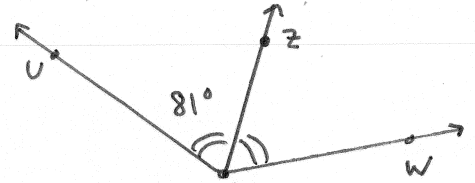
$$x = 9$$

$$m\angle PMN = 5(9) + 5 = 50$$

$$\boxed{m\angle PMN = 50^\circ}$$



21.  $\vec{VZ}$  bisects  $\angle UVW$ , and  $m\angle UVZ = 81^\circ$ . Find  $m\angle UVW$ . Then classify  $\angle UVW$  by its angle measure.



$$m\angle UVW = 162^\circ$$

Obtuse

$\angle 1$  and  $\angle 2$  are complementary angles. Given the measure of  $\angle 1$ , find  $m\angle 2$ .

22.  $m\angle 1 = 12^\circ$   
 $12 + m\angle 2 = 90$

$$m\angle 2 = 78^\circ$$

23.  $m\angle 1 = 83^\circ$   
 $83 + m\angle 2 = 90$

$$m\angle 2 = 7^\circ$$

24.  $m\angle 1 = 46^\circ$   
 $46 + m\angle 2 = 90$

$$m\angle 2 = 44^\circ$$

25.  $m\angle 1 = 2^\circ$   
~~102~~  $2 + m\angle 2 = 90$

$$m\angle 2 = 88^\circ$$

$\angle 3$  and  $\angle 4$  are supplementary angles. Given the measure of  $\angle 3$ , find  $m\angle 4$ .

26.  $m\angle 3 = 116^\circ$   
 $116 + m\angle 4 = 180$

$$m\angle 4 = 64^\circ$$

27.  $m\angle 3 = 56^\circ$   
 $56 + m\angle 4 = 180$

$$m\angle 4 = 124^\circ$$

28.  $m\angle 3 = 89^\circ$   
 $89 + m\angle 4 = 180$

$$m\angle 4 = 91^\circ$$

29.  $m\angle 3 = 12^\circ$   
 $12 + m\angle 4 = 180$

$$m\angle 4 = 168^\circ$$

30.  $\angle 1$  and  $\angle 2$  are complementary angles. Find the measures of the angles when  $m\angle 1 = (x - 10)^\circ$  and  $m\angle 2 = (2x + 40)^\circ$ .

$$\begin{aligned} x - 10 + 2x + 40 &= 90 \\ 3x + 30 &= 90 \\ 3x &= 60 \end{aligned}$$

$$x = 20$$

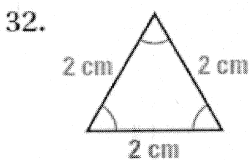
$$\begin{aligned} m\angle 1 &= 10^\circ \\ m\angle 2 &= 80^\circ \end{aligned}$$

31.  $\angle 1$  and  $\angle 2$  are supplementary angles. Find the measures of the angles when  $m\angle 1 = (3x + 50)^\circ$  and  $m\angle 2 = (4x + 32)^\circ$ . Then classify  $\angle 1$  by its angle measure.

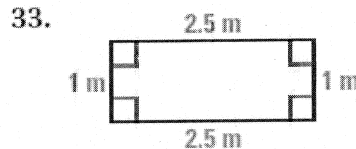
$$\begin{aligned} 3x + 50 + 4x + 32 &= 180 \\ 7x + 82 &= 180 \\ 7x &= 98 \\ x &= 14 \end{aligned}$$

$$m\angle 1 = 92^\circ$$

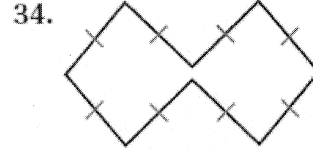
$$m\angle 2 = 88^\circ$$



Triangle; regular b/c it is equiangular and equilateral

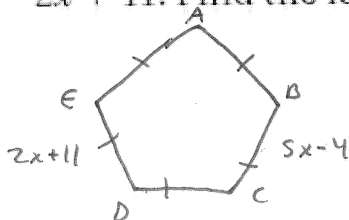


Quadrilateral; Equiangular b/c it has 4  $\cong$   $\angle$ 's, but not all sides are  $\cong$



Octagon; Equilateral b/c all 8 sides are  $\cong$ , but not all  $\angle$ 's are  $\cong$ .

35. Pentagon  $ABCDE$  is a regular polygon. The length of  $\overline{BC}$  is represented by the expression  $5x - 4$ . The length of  $\overline{DE}$  is represented by the expression  $2x + 11$ . Find the length of  $\overline{AB}$ .

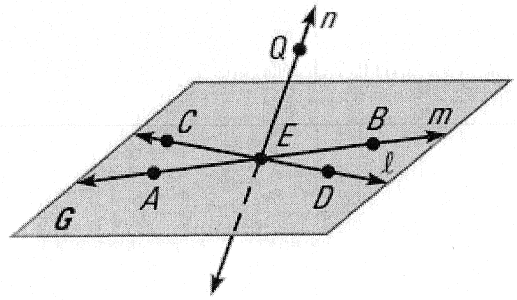


$$\begin{aligned} 5x - 4 &= 2x + 11 \\ 3x &= 15 \\ x &= 5 \end{aligned}$$

$$AB = 21$$

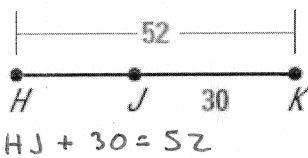
Use the diagram to decide whether the statement is true or false.

1. Point A lies on line  $m$ . true
2. Point D lies on line  $n$ . false
3. Points B, C, E, and Q are coplanar. false
4. Points C, E, and B are collinear. false
5. Another name for plane G is plane QEC. false



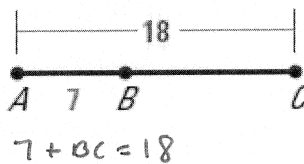
Find the indicated length.

6. Find  $HJ$ .



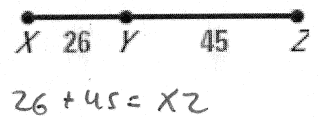
$$HJ = 22$$

7. Find  $BC$ .



$$BC = 11$$

8. Find  $XZ$ .



$$XZ = 71$$

In Exercises 9–11, find the distance between the two points.

9.  $T(3, 4)$  and  $W(2, 7)$

$$d = \sqrt{(2-3)^2 + (7-4)^2}$$

$$= \sqrt{(-1)^2 + (3)^2}$$

$$= \sqrt{10}$$

$$TW = \sqrt{10} \approx 3.16$$

10.  $C(5, 10)$  and  $D(6, -1)$

$$d = \sqrt{(6-5)^2 + (-1-10)^2}$$

$$= \sqrt{(1)^2 + (-11)^2}$$

$$= \sqrt{122}$$

$$CD = \sqrt{122} \approx 11.05$$

11.  $M(-8, 0)$  and  $N(-1, 3)$

$$d = \sqrt{(-1-(-8))^2 + (3-0)^2}$$

$$= \sqrt{(7)^2 + (3)^2}$$

$$= \sqrt{58}$$

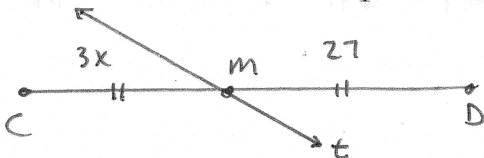
$$MN = \sqrt{58} \approx 7.62$$

12. The midpoint of  $AB$  is  $M(9, 7)$ . One endpoint is  $A(3, 9)$ . Find the coordinates of endpoint  $B$ .

$$\left. \begin{aligned} \frac{3+x_1}{2} &= 9 \\ \frac{9+y_1}{2} &= 7 \end{aligned} \right\} \begin{aligned} x_1 &= 15 \\ y_1 &= 5 \end{aligned}$$

$$B(15, 5)$$

13. Line  $t$  bisects  $CD$  at point  $M$ ,  $CM = 3x$ , and  $MD = 27$ . Find  $CD$ .



$$CD = 54$$

In Exercises 15, use the diagram.

15. Given  $m\angle KHJ = 90^\circ$ , find  $m\angle LHJ$ .

$$m\angle LHJ = 4(7) + 7$$

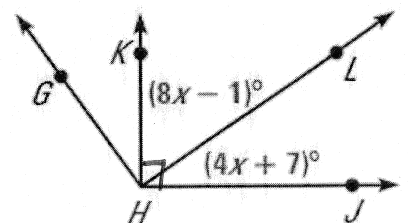
$$m\angle LHJ = 35^\circ$$

$$8x - 1 + 4x + 7 = 90$$

$$12x + 6 = 90$$

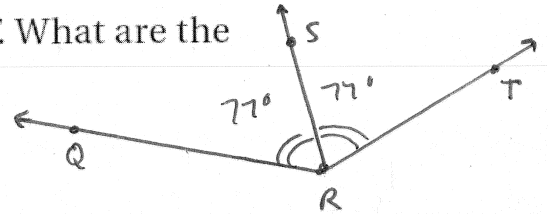
$$12x = 84$$

$$x = 7$$



16. The measure of  $\angle QRT$  is  $154^\circ$ , and  $\overline{RS}$  bisects  $\angle QRT$ . What are the measures of  $\angle QRS$  and  $\angle SRT$ ?

$$\begin{aligned} m\angle QRS &= 77^\circ \\ m\angle SRT &= 77^\circ \end{aligned}$$



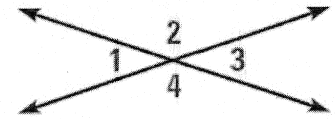
In Exercises 17 and 18, use the diagram at the right.

17. Name four linear pairs.

$$\angle 1 + \angle 2; \angle 2 + \angle 3; \angle 3 + \angle 4; \angle 4 + \angle 1$$

18. Name two pairs of vertical angles.

$$\angle 1 + \angle 3; \angle 2 + \angle 4$$

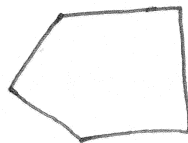


19. The measure of an angle is  $64^\circ$ . What is the measure of its complement? What is the measure of its supplement?

$$\text{Complement} = 26^\circ$$

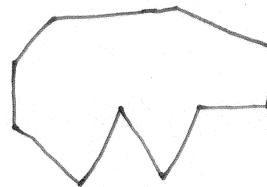
$$\text{Supplement} = 116^\circ$$

20. A convex polygon has half as many sides as a concave 10-gon. Draw the concave polygon and the convex polygon. Classify the convex polygon by the number of sides it has.



convex

Pentagon (5 sides)



concave

Decagon (10-sides)